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# A Rigorous Analytical Framework for the Dispersion Strategy

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*“Harmony with Uncertainty”*

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*A stylized example:*

Consider an index consisting of 2 equally weighted stocks:

$$X = \frac{S_1 + S_2}{2}$$

Assume the annualized volatility of both stocks are 30:

1. Perfect anti-correlation:  $\text{Var}(X) = 0$ ,  $\text{Vol}(X) = 0$

2. Zero correlation:  $\text{Var}(X) = \frac{\text{Var}(S_1) + \text{Var}(S_2)}{4} = 450$ ,  $\text{Vol}(X) \approx 21$

3. Perfect correlation:

$$\text{Var}(X) = \frac{\text{Var}(S_1) + \text{Var}(S_2) + 2\sqrt{\text{Var}(S_1)}\sqrt{\text{Var}(S_2)}}{4} = 900, \text{Vol}(X) = 30$$

What is the dispersion trade?

- Long single stock volatilities,
- Short the corresponding index volatility

Why long dispersion?

- Index vols are rich
  - .....▶ *Primary hedging instrument: index puts.*
- The median implied volatility risk premium (6m ATM implied vol – subsequent realized vol) for the SPX is 3 since 2005. The average for the S&P large cap stocks is 1.6.

- ❑ How to measure the attractiveness of a dispersion position?
- ❑ Common heuristics: **Implied Correlation**
- ❑ Index return is a weighted sum of single stocks returns:

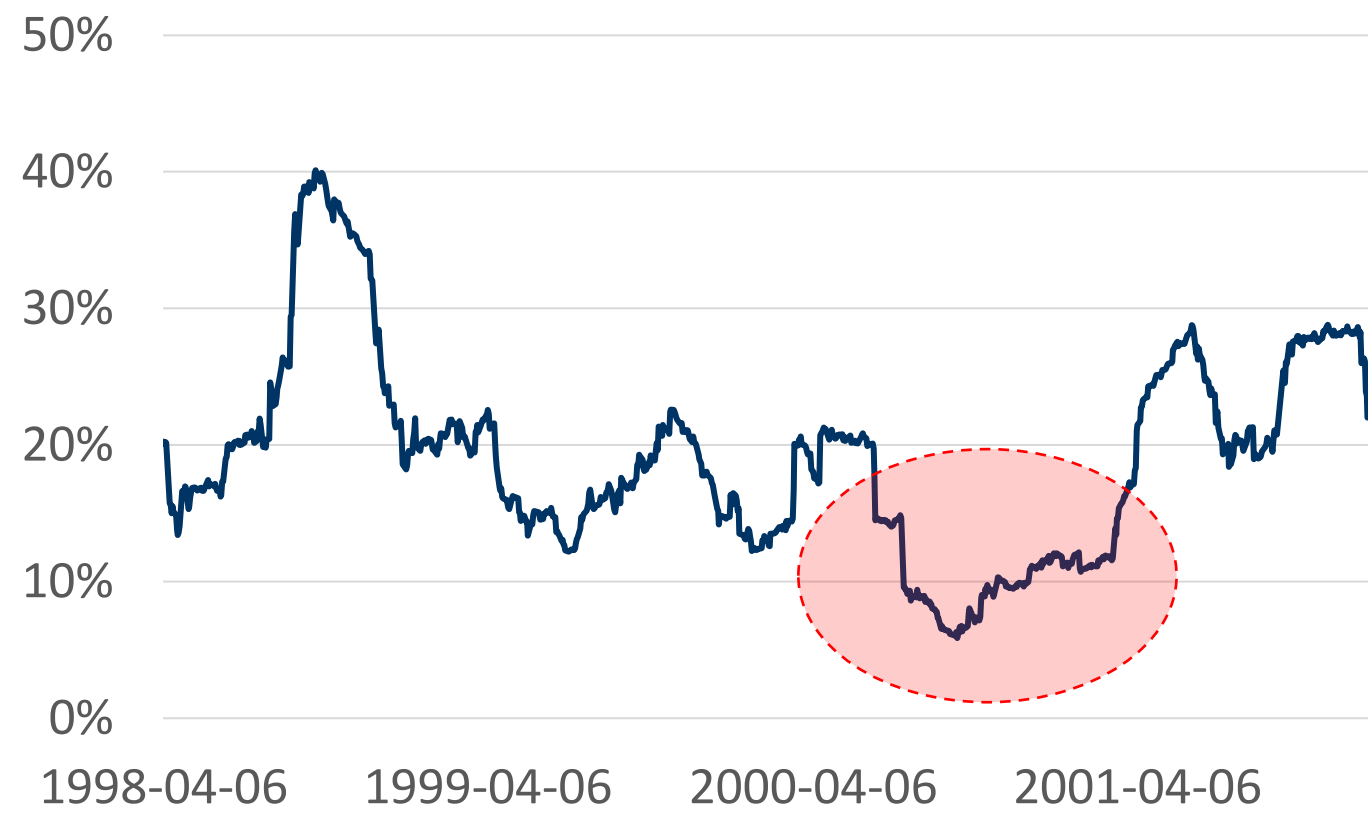
$$X = \sum w_i S_i$$

- ❑ Assuming the correlation between any pair of distinct stocks to be the same number  $\rho$ , then for a sufficiently diversified index:

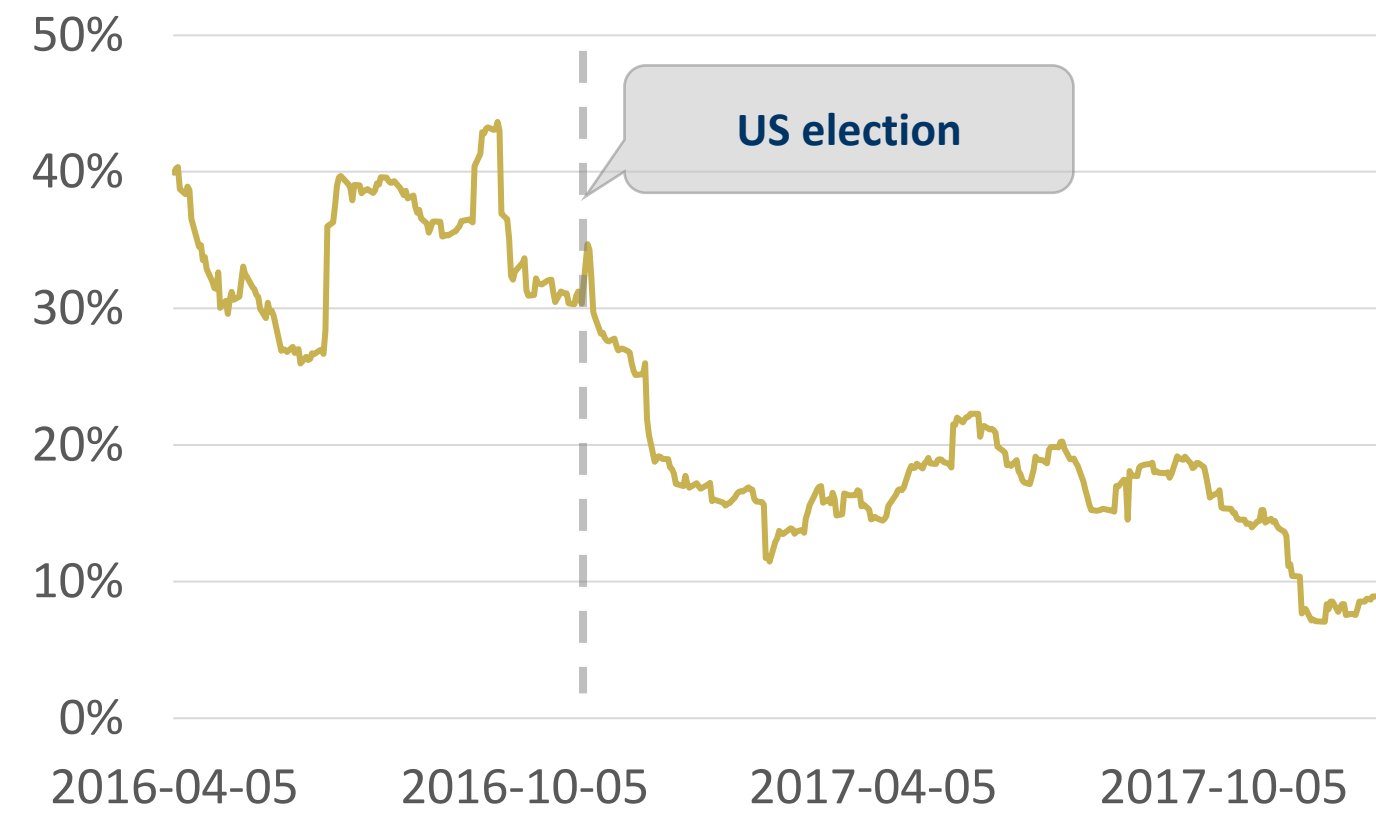
$$\rho \approx \frac{\text{Var}(X)}{\left(\sum w_i \sqrt{\text{Var}(S_i)}\right)^2} = \left(\frac{\text{Index vol}}{\text{Average Stock vol}}\right)^2$$

# Realized Average Correlation

SPX top 100 3m average realized correlation



SPX top 100 3m average realized correlation



*Advantage: intuitive & easy to apply*

*Disadvantage: simplistic & operationally inflexible*

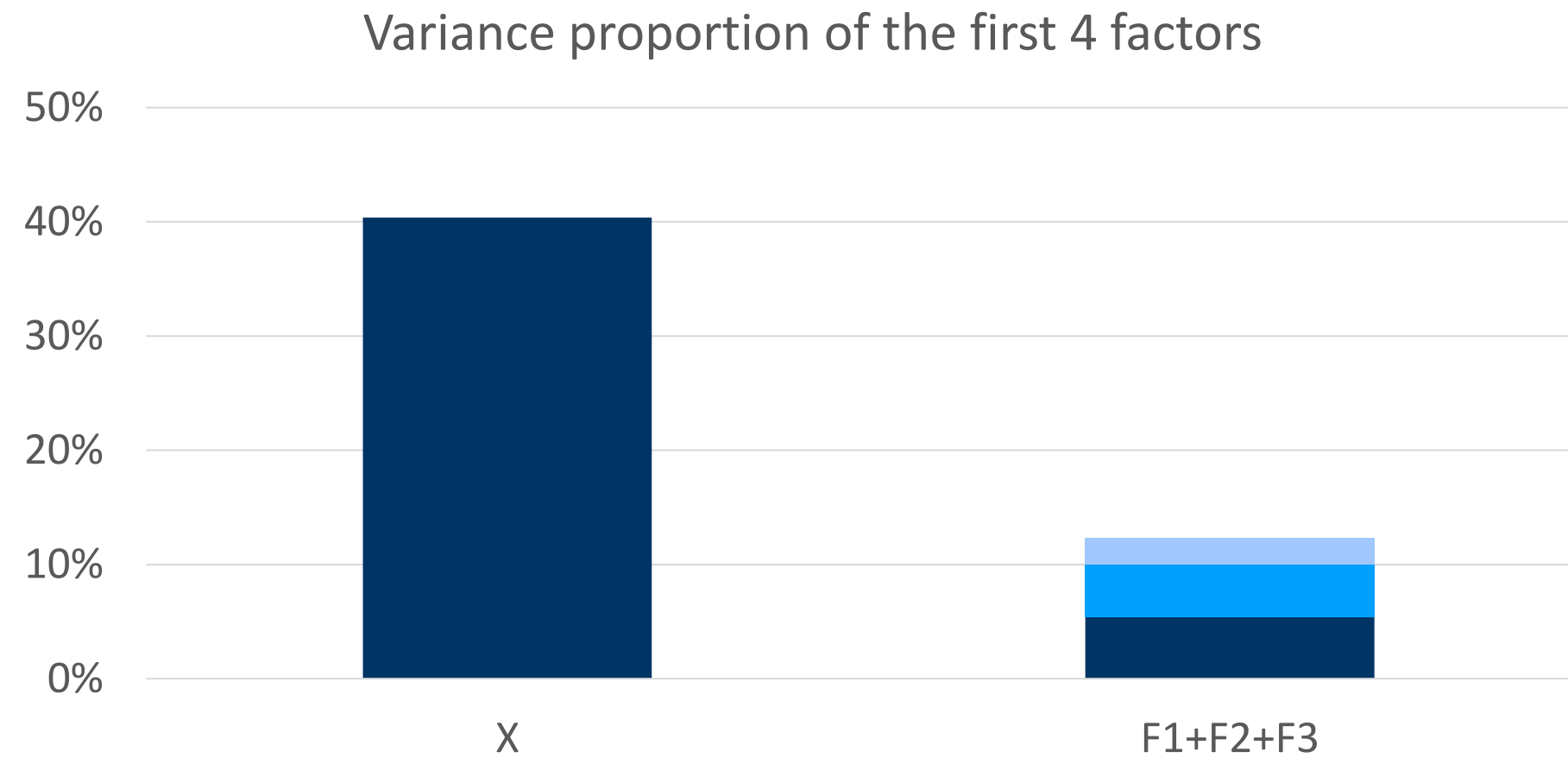
1. Use 1 variable to proxy the entire covariance matrix
2. It presupposes a one-factor model on single stock returns:

$$S = \beta X + \varepsilon,$$

$X$ : macro/market return

$\varepsilon$ : the company-specific idiosyncratic return

3. Each stock is assumed to have the same correlation with the common factor  $X$
4. Cannot assess the cheapness of individual single stock vols vis-à-vis index



- ❑ X: main factor, correlation with SPX > 0.98
- ❑ F1 + F2 + F3 explain > 10% variance
- ❑ One factor is inadequate

- Single stock returns can be decomposed as:

$$S = \beta X + c_1 F_1 + c_2 F_2 + c_3 F_3 + \varepsilon,$$

$X$ : macro/market return

$F_1$ : cyclical/defensive factor

$F_2$ : momentum factor

$F_3$ : growth/value factor

$\varepsilon$ : the company-specific idiosyncratic return

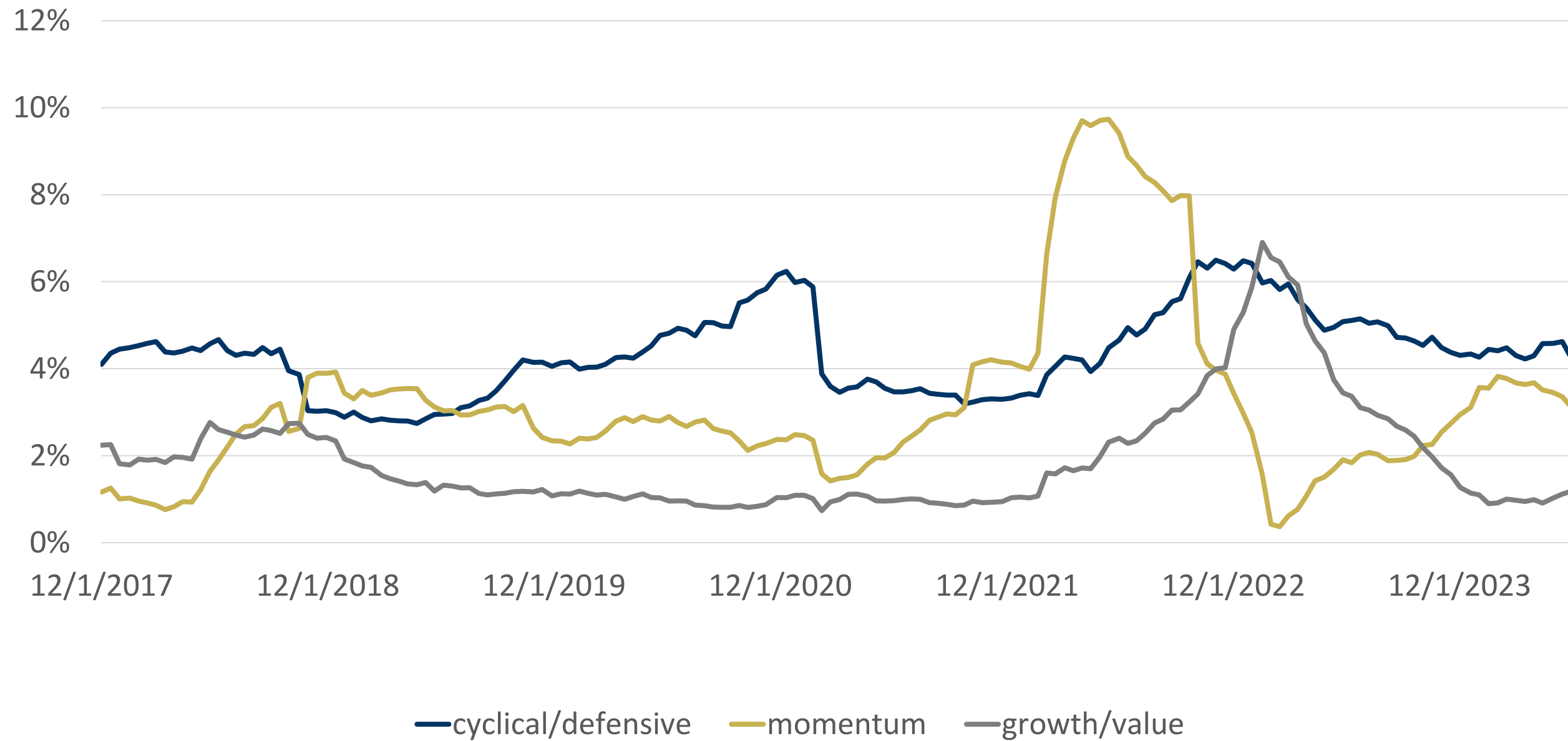
- Consequently:

$$\text{Var}(S) = \beta^2 \text{Var}(X) + c_1^2 \text{Var}(F_1) + c_2^2 \text{Var}(F_2) + c_3^2 \text{Var}(F_3) + \text{Var}(\varepsilon)$$

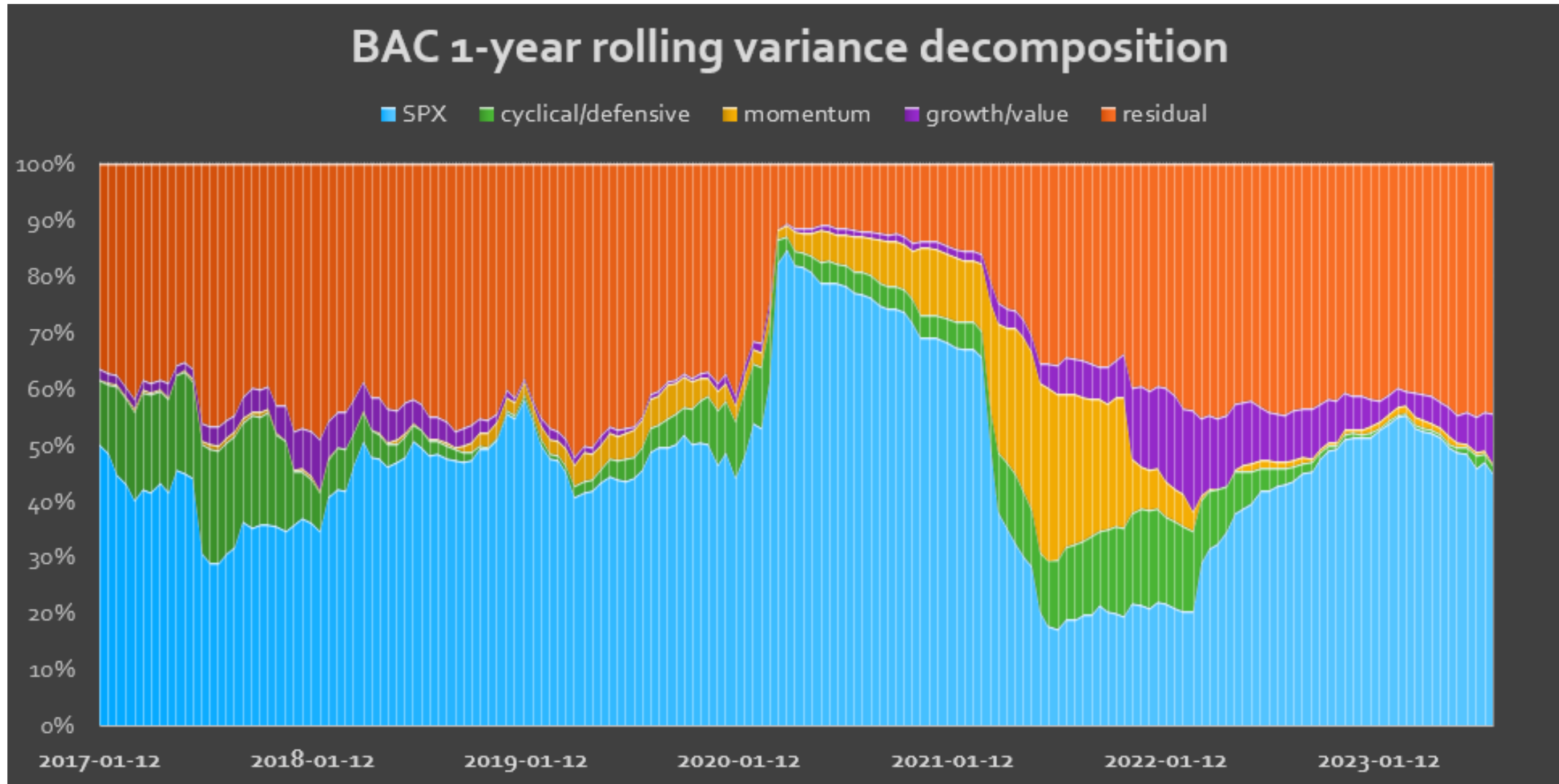


# The Other Factors

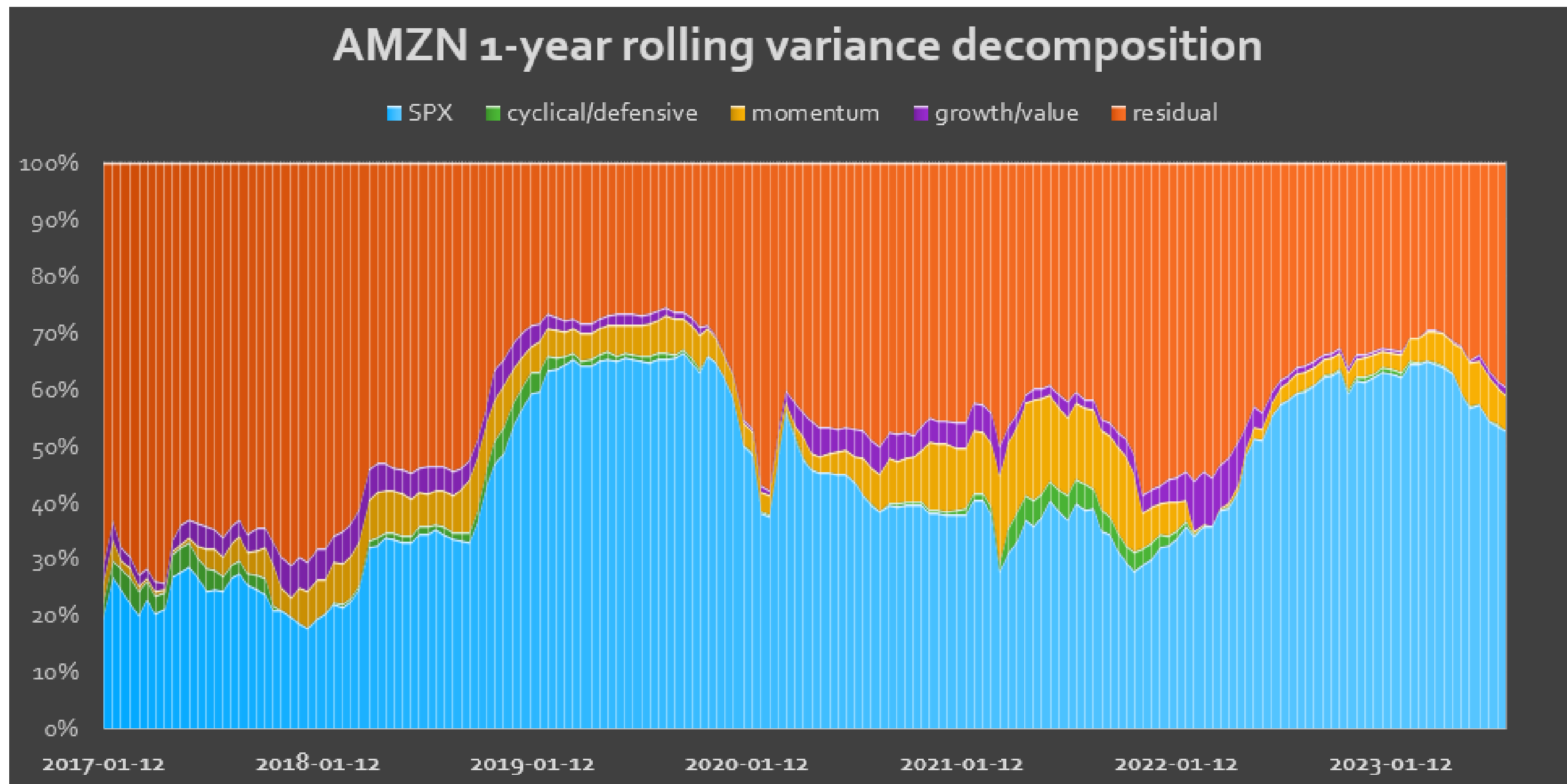
Average % of single stock variance explained by factors



# Temporal Evolution of Factors



# Temporal Evolution of Factors



- Payoff of a portfolio consisting of long single stock vol positions and short index vol positions is:

$$\begin{aligned} & \Sigma w_i \text{Var}(S_i) - (\Sigma w_i \beta_i^2) \text{Var}(X) \\ &= \Sigma w_i \left( c_{1,i}^2 \text{Var}(F_1) + c_{2,i}^2 \text{Var}(F_2) + c_{3,i}^2 \text{Var}(F_3) + \text{Var}(\varepsilon_i) \right), \end{aligned}$$

which has zero exposure to the volatility of the broad market while long the volatility of the individual factors as well as the idiosyncratic returns.

- Payoff of a portfolio consisting of long single stock vol swaps and short index vol swap in a theta-neutral fashion is :

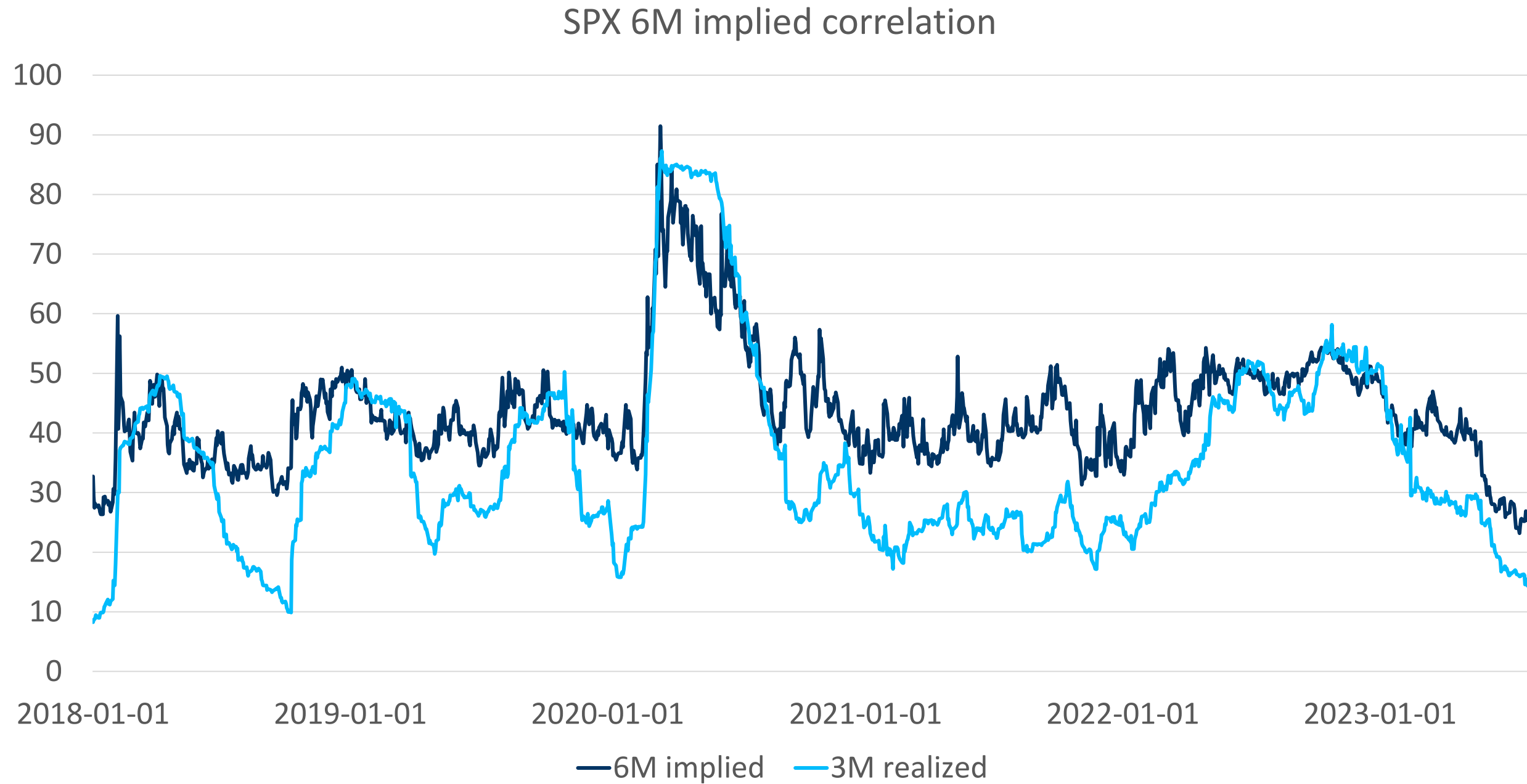
$$\frac{1}{\sqrt{\rho_i}} \times \text{Average Stock Realized Vol} \times (\sqrt{\rho_i} - \sqrt{\rho_r})$$

- Payoff of a portfolio consisting of long single stock var swaps and short index var swap in a theta-neutral fashion is :

$$\frac{1}{\rho_i} \times \text{Average Stock Realized Variance} \times (\rho_i - \rho_r)$$

- In a crash/distress scenario, realized vols and correlation invariably rise together, the left tail of the p&l distribution can be very heavy indeed.

# Implied Correlation Time Series



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